## Sequence Alignment

#### Outline

- Global Alignment
- Scoring Matrices
- Local Alignment
- Alignment with Affine Gap Penalties

#### From LCS to Alignment: Change up the Scoring

- The Longest Common Subsequence (LCS) problem
   —the simplest form of sequence alignment allows
   only insertions and deletions (no mismatches).
- In the LCS Problem, we scored 1 for matches and 0 for indels
- Consider penalizing indels and mismatches with negative scores
- Simplest scoring schema:
  - +1: match premium
  - -µ: mismatch penalty
  - -σ: indel penalty

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## Simple Scoring

 When mismatches are penalized by –μ, indels are penalized by –σ, and matches are rewarded with +1, the resulting score is:

 $\#matches - \mu(\#mismatches) - \sigma(\#indels)$ 

## The Global Alignment Problem

Find the best alignment between two strings under a given scoring schema

Input: Strings v and w and a scoring schema

Output: Alignment of maximum score

$$\uparrow \rightarrow = -6$$

$$= 1 \text{ if match}$$

$$\begin{cases} = -\mu \text{ if mismatch} \end{cases}$$

$$m : \text{mismatch}$$

$$s_{i-1,j-1} + 1 \text{ if } v_i = w_j$$

$$s_{i,j} = \max \quad s_{i-1,j-1} - \mu \text{ if } v_i \neq w_j$$

$$s_{i-1,j} - \sigma$$

$$s_{i,j-1} - \sigma$$

## Scoring Matrices

To generalize scoring, consider a  $(4+1) \times (4+1)$  scoring matrix  $\delta$ .

In the case of an amino acid sequence alignment, the scoring matrix would be a (20+1)x(20+1) size. The addition of 1 is to include the score for comparison of a gap character "-".

This will simplify the algorithm as follows:

$$s_{i-1,j-1} + \delta(v_i, w_j)$$

$$s_{i,j} = \max \quad s_{i-1,j} + \delta(v_i, -)$$

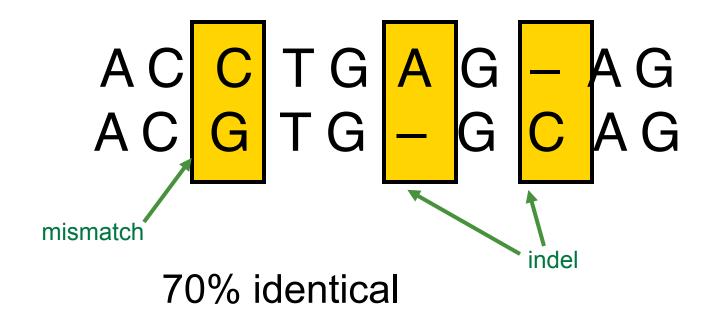
$$s_{i,j-1} + \delta(-, w_j)$$

## Measuring Similarity

- Measuring the extent of similarity between two sequences
  - Based on percent sequence <u>identity</u>
  - Based on conservation

#### Percent Sequence Identity

 The extent to which two nucleotide or amino acid sequences are invariant



### Making a Scoring Matrix

- Scoring matrices are created based on biological evidence.
- Alignments can be thought of as two sequences that differ due to mutations.
- Some of these mutations have little effect on the protein's function, therefore some penalties,  $\delta(v_i, w_j)$ , will be less harsh than others.

### Scoring Matrix: Example

	А	R	N	K
Α	5	-2	-1	-1
R	-	7	-1	<u>က</u>
N	-	_	7	0
K	-	-	-	6

AKRANR KAAANK

- Notice that although R and K are different amino acids, they have a positive score.
- Why? They are both positively charged amino acidsà will not greatly change function of protein.

#### Conservation

- Amino acid changes that tend to preserve the physico-chemical properties of the original residue
  - Polar to polar
    - aspartate à glutamate
  - Nonpolar to nonpolar
    - alanine à valine
  - Similarly behaving residues
    - leucine to isoleucine

## Scoring matrices

- Amino acid substitution matrices
  - PAM
  - BLOSUM

- DNA substitution matrices
  - DNA is less conserved than protein sequences
  - Less effective to compare coding regions at nucleotide level

#### PAM

- Point Accepted Mutation (Dayhoff et al.)
- 1 PAM = PAM<sub>1</sub> = 1% average change of all amino acid positions
  - After 100 PAMs of evolution, not every residue will have changed
    - some residues may have mutated several times
    - some residues may have returned to their original state
    - some residues may not changed at all

# PAMX

- $PAM_X = PAM_1^X$ 
  - $PAM_{250} = PAM_1^{250}$
- PAM<sub>250</sub> is a widely used scoring matrix:

	Ala	Arg	Asn	Asp	Cys	Gln	Glu	Gly	His	Ile	Leu	Lys	
	A	R	N	D	С	Q	${ m E}$	G	Н	I	L	K	
Ala A	13	6	9	9	5	8	9	12	6	8	6	7	
Arg R	3	17	4	3	2	5	3	2	6	3	2	9	
Asn N	4	4	6	7	2	5	6	4	6	3	2	5	
Asp D	5	4	8	11	1	7	10	5	6	3	2	5	
Cys C	2	1	1	1	52	1	1	2	2	2	1	1	
Gln Q	3	5	5	6	1	10	7	3	7	2	3	5	
• • •													
Trp W	0	2	0	0	0	0	0	0	1	0	1	0	
Tyr Y	1	1	2	1	3	1	1	1	3	2	2	1	
Val V	7	4	4	4	4	4	4	4	5	4	15	10	

#### **BLOSUM**

- Blocks Substitution Matrix
- Scores derived from observations of the frequencies of substitutions in blocks of local alignments in related proteins
- Matrix name indicates evolutionary distance
  - BLOSUM62 was created using sequences sharing no more than 62% identity

### The Blosum50 Scoring Matrix

| 7<br>1 -1<br>2 -2 | -1<br>-1<br>7  | -2<br>-2  | -1<br>-4   | -1  | -1   | 0  | - 2  
  | _  |  |  
   
  |  
   |   |  |  |  |   |  
  |  |  |   |  |    |
|-------------------|--|---|--|---|--|--
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--|---|--|--|--|---|---|--
--|---|--|----|
| -1                | H  | =   | _4   |   |  | _  | -2   
  | -1   | -2   | -1   
   
  | -1   
   | -3  | -1   | 1  | 0  | -3  | -2   
  | 0  | -2   | -1  | -1   | -5 |
| 2 -2              | 7  |   | •  | 1   | 0  | -3   | 0  
  | -4   | -3   | 3  
   
  | -2   
   | -3  | -3   | -1   | -1   | -3  | -1   
  | -3   | -1   | 0   | -1   | -5 |
|                   |  | 2   | -2   | 0   | 0  | 0  | 1  
  | -3   | -4   | 0  
   
  | -2   
   | -4  | -2   | 1  | 0  | -4  | -2   
  | -3   | 4  | 0   | -1   | -5 |
|                   | 2  | 8   | -4   | 0   | 2  | -1   | -1   
  | -4   | -4   | -1   
   
  | -4   
   | -5  | -1   | 0  | -1   | -5  | -3   
  | -4   | 5  | 1   | -1   | -5 |
| l  -4             | -2   | -4  | 13   | -3  | -3   | -3   | -3   
  | -2   | -2   | -3   
   
  | -2   
   | -2  | -4   | -1   | -1   | -5  | -3   
  | -1   | -3   | -3  | -2   | -5 |
| 1                 | 0  | 0   | -3   | 7   | 2  | -2   | 1  
  | -3   | -2   | 2  
   
  | 0  
   | -4  | -1   | 0  | -1   | -1  | -1   
  | -3   | 0  | 4   | -1   | -5 |
| 0                 | 0  | 2   | -3   | 2   | 6  | -3   | 0  
  | -4   | -3   | 1  
   
  | -2   
   | -3  | -1   | -1   | -1   | -3  | -2   
  | -3   | 1  | 5   | -1   | -5 |
| -3                | 0  | -1  | -3   | -2  | -3   | 8  | -2   
  | -4   | -4   | -2   
   
  | -3   
   | -4  | -2   | 0  | -2   | -3  | -3   
  | -4   | -1   | -2  | -2   | -5 |
| 2 0               | 1  | -1  | -3   | 1   | 0  | -2   | 10   
  | -4   | -3   | 0  
   
  | -1   
   | -1  | -2   | -1   | -2   | -3  | 2  
  | -4   | 0  | 0   | -1   | -5 |
| l -4              | -3   | -4  | -2   | -3  | -4   | -4   | -4   
  | 5  | 2  | -3   
   
  | 2  
   | 0   | -3   | -3   | -1   | -3  | -1   
  | 4  | -4   | -3  | -1   | -5 |
| 2 -3              | -4   | -4  | -2   | -2  | -3   | -4   | -3   
  | 2  | 5  | -3   
   
  | 3  
   | 1   | -4   | -3   | -1   | -2  | -1   
  | 1  | -4   | -3  | -1   | -5 |
| 3                 | 0  | -1  | -3   | 2   | 1  | -2   | 0  
  | -3   | -3   | 6  
   
  | -2   
   | -4  | -1   | 0  | -1   | -3  | -2   
  | -3   | 0  | 1   | -1   | -5 |
| -2                | -2   | -4  | -2   | 0   | -2   | -3   | -1   
  | 2  | 3  | -2   
   
  | 7  
   | 0   | -3   | -2   | -1   | -1  | 0  
  | 1  | -3   | -1  | -1   | -5 |
| -3                | -4   | -5  | -2   | -4  | -3   | -4   | -1   
  | 0  | 1  | -4   
   
  | 0  
   | 8   | -4   | -3   | -2   | 1   | 4  
  | -1   | -4   | -4  | -2   | -5 |
| -3                | -2   | -1  | -4   | -1  | -1   | -2   | -2   
  | -3   | -4   | -1   
   
  | -3   
   | -4  | 10   | -1   | -1   | -4  | -3   
  | -3   | -2   | -1  | -2   | -5 |
| -1                | 1  | 0   | -1   | 0   | -1   | 0  | -1   
  | -3   | -3   | 0  
   
  | -2   
   | -3  | -1   | 5  | 2  | -4  | -2   
  | -2   | 0  | 0   | -1   | -5 |
| -1                | 0  | -1  | -1   | -1  | -1   | -2   | -2   
  | -1   | -1   | -1   
   
  | -1   
   | -2  | -1   | 2  | 5  | -3  | -2   
  | 0  | 0  | -1  | 0  | -5 |
| -3                | -4   | -5  | -5   | -1  | -3   | -3   | -3   
  | -3   | -2   | -3   
   
  | -1   
   | 1   | -4   | -4   | -3   | 15  | 2  
  | -3   | -5   | -2  | -3   | -5 |
| 2 -1              | -2   | -3  | -3   | -1  | -2   | -3   | 2  
  | -1   | -1   | -2   
   
  | 0  
   | 4   | -3   | -2   | -2   | 2   | 8  
  | -1   | -3   | -2  | -1   | -5 |
| -3                | -3   | -4  | -1   | -3  | -3   | -4   | -4   
  | 4  | 1  | -3   
   
  | 1  
   | -1  | -3   | -2   | 0  | -3  | -1   
  | 5  | -4   | -3  | -1   | -5 |
| 2 -1              | 4  | 5   | -3   | 0   | 1  | -1   | 0  
  | -4   | -4   | 0  
   
  | -3   
   | -4  | -2   | 0  | 0  | -5  | -3   
  | -4   | 5  | 2   | -1   | -5 |
| 0                 | 0  | 1   | -3   | 4   | 5  | -2   | 0  
  | -3   | -3   | 1  
   
  | -1   
   | -4  | -1   | 0  | -1   | -2  | -2   
  | -3   | 2  | 5   | -1   | -5 |
| -1                | -1   | -1  | -2   | -1  | -1   | -2   | -1   
  | -1   | -1   | -1   
   
  | -1   
   | -2  | -2   | -1   | 0  | -3  | -1   
  | -1   | -1   | -1  | -1   | -5 |
| 5 -5              | -5   | -5  | -5   | -5  | -5   | -5   | -5   
  | -5   | -5   | -5   
   
  | -5   
   | -5  | -5   | -5   | -5   | -5  | -5   
  | -5   | -5   | -5  | -5   | 1  |
|                   | 0<br>-3<br>0<br>-4<br>-3<br>3<br>-2<br>-3<br>-1<br>-1<br>-1<br>-3<br>-1<br>0<br>-1 | 0 0 1 -4 -3 -4 -3 -4 -3 -2 -1 1 -1 0 0 0 -1 -1 -1 | 0 0 2<br>-3 0 -1<br>0 1 -1<br>-4 -3 -4<br>-3 -4 -4<br>3 0 -1<br>-2 -2 -4<br>-3 -4 -5<br>-3 -2 -1<br>-1 0 -1<br>-3 -4 -5<br>-1 0 -1<br>-3 -4 -5<br>-1 0 -1<br>-3 -4 -5<br>-1 0 0 1<br>-1 0 0 1<br>-1 -1 -1 -1 | 0     0     2     -3       -3     0     -1     -3       0     1     -1     -3       -4     -3     -4     -2       3     0     -1     -3       -2     -2     -4     -2       -3     -4     -5     -2       -3     -2     -1     -4       -1     1     0     -1       -1     0     -1     -1       -3     -4     -5     -5       -1     -2     -3     -3       -3     -3     -4     -1       -1     4     5     -3       0     0     1     -3       -1     -1     -1     -2 | 0 0 2 -3 2 -3 0 -1 -3 -2 0 1 -1 -3 1 -4 -3 -4 -2 -3 -3 -4 -4 -2 -2 3 0 -1 -3 2 -2 -2 -4 -2 0 -3 -4 -5 -2 -4 -3 -2 -1 -4 -1 -1 0 -1 0 -1 0 -1 -1 -1 -3 -4 -5 -5 -1 -1 -2 -3 -3 -1 -3 -3 -4 -1 -3 -1 4 5 -3 0 0 0 1 -3 4 -1 -1 -1 -1 -2 -1 | 0         0         2         -3         2         6           -3         0         -1         -3         -2         -3           0         1         -1         -3         1         0           -4         -3         -4         -2         -3         -4           -3         -4         -4         -2         -2         -3           3         0         -1         -3         2         1           -2         -2         -4         -2         0         -2           -3         -4         -5         -2         -4         -3           -3         -2         -1         -4         -1         -1           -1         0         -1         -1         -1         -1           -1         0         -1         -1         -1         -1           -3         -4         -5         -5         -1         -3           -1         -2         -3         -3         -1         -2           -3         -3         -4         -1         -3         -3           -1         4         5         -3         0         < | 0         0         2         -3         2         6         -3           -3         0         -1         -3         -2         -3         8           0         1         -1         -3         1         0         -2           -4         -3         -4         -2         -3         -4         -4           -3         -4         -4         -2         -2         -3         -4           3         0         -1         -3         2         1         -2           -2         -2         -4         -2         0         -2         -3           -3         -4         -5         -2         -4         -3         -4           -3         -2         -1         -4         -1         -1         -2           -1         1         0         -1         0         -1         0         0         1         0           -1         0         -1         -1         -1         -1         -1         -2         -3           -3         -3         -3         -1         -2    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        -3         -2         -3         8         -2         -4           0         1         -1         -3         1         0         -2         10         -4           -4         -3         -4         -2         -3         -4         -4         -5           -3         -4         -4         -2         -2         -3         -4         -3         2           -3         -4         -4         -2         -2         -3         -4         -3         2           -3         -4         -4         -2         -2         -3         -4         -3         2           -3         -4         -5         -2         -4         -3         -4         -1         0           -3         -4         -5         -2         -4         -3         -4         -1         0           -3         -2         -1         -4         -1         -1         -2         -2         -3           -1         0         -1         -1</th><th>0         0         2         -3         2         6         -3         0         -4         -3           -3         0         -1         -3         -2         -3         8         -2         -4         -4            0         1         -1         -3         1         0         -2         10         -4         -3           -4         -3         -4         -2         -3         -4         -4         -4         5         2           -3         -4         -4         -2         -2         -3         -4         -3         2         5           3         0         -1         -3         2         1         -2         0         -3         -3           -2         -2         -4         -2         0         -2         -3         -1         2         3           -3         -4         -5         -2         -4         -3         -4         -1         0         1           -3         -4         -5         -2         -4         -3         -4         -1         0         1           -3         -4         -5         -5         <td< th=""><th>0         0         2         -3         2         6         -3         0         -4         -3         1           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2           0         1         -1         -3         1         0         -2         10         -4         -3         0           -4         -3         -4         -2         -3         -4         -4         -5         2         -3           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3           3         0         -1         -3         2         1         -2         0         -3         -3         6           -2         -2         -4         -2         0         -2         -3         -1         2         3         -2           -3         -4         -5         -2         -4         -3         -4         -1         0         1         -4           -3         -2         -1         -4         -1         -1         -1         -1         <td< th=""><th>0      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   -2           -4         -3         -4         -2         -3         -4         -4         -4         5         2         -3         2         0         -3           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3         3         1         -4           3         0         -1         -3         2         1         -2         0         -3      
  -3         6         -2         -4         -1           -2         -2         -4         -2         0         -2         -3         -1         2         3         -2         7         0         -3</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1           -4         -3         -4         -2         -3         -4         -4         -4         5         2         -3         2         0         -3         -3           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3         3         1         -4         -3           3         0         -1         -3         2         1         -2         0         -3         -3         6         -2         -4         -1         0           -2         -2         -4         -3         -1         2         3         -</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -2         0         -2         -1         -2         -3         -4         -2         -2         -1         -2         -1         -2         -1         -2         -1         -2         -1         -2         -3         -3         -1         -2         -3         -1         -3         -1         -3         -4         -3         -1         -3         -4         -3         -1         -3         -3         -1         -3         -1         -3         -1         -3         -1         -3         -1         -3         -1         -3         -2         -1         -1         -1         -1         -1         -1         -1</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -1         -3         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -4         -2         0         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -3         -3         -1         -3         -4         -3         -2         -3         2         0         -3         -3         -1         -2         -3         -1         -3         -4         -3         -1         -2         -2         -4         -1         0         -1         -3         -1         -2         -2         -4         -1         0         -1         -3         -2         -1         -1         -1         -1         &lt;</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -3           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1         -2         -3         2           -4         -3         -4         -4         -4         5         2         -3         2         0         -3         -3         -1         -3         -1         -3         -1         -2         -1         -3         -1         -2         -1         -3         -1         -2         -3         -3         1         -4         -3         -1         -2         -1           -3         -4         -4         -2         -2         -3         -1         2         3         -2         7         0         -3         -2         -1         -1         0</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -4           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1         -2         -3         2         -4           -4         -3         -4         -2         -3         -4         -4         -4         5         2         -3         2         0         -3         -3         -1         -2         -1         1           -3         -4         -4         -2         -2         -3         -4         -3         -2         -3         3         1         -4         -3         -1         -2         -1         1           3         0         -1         -3         -3         -3         -2         -4         -1         0         -1         -3         -2</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -4         -1           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1         -2         -3         2         -4         0           -4         -3         -4         -2         -3         -4         -4         -4         -5         2         -3         2         0         -3         -3         -1         -3         -1         -4         -3         -1         -2         -1         1         -4         -3         -1         -2<th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         1         -2         -3         -1         -1         -3         -2         -3         -4         -1         -2         0         -2         -3         -3         -4         -1         -2         0         -2         -3         -3         -4         -1         -2         0         0         -2         -3         -3         0         -1         -1         -2         -3         2         -4         0         0         0         -2         -3         -4         -4         -3         0         -1         -2         -3         2         -4         0         0         0         -4         -3         -2         -1         -1         0</th><th>  0</th></th></td<></th></td<></th></td<> | 0     0     2     -3     2     6     -3     0       -3     0     -1     -3     -2     -3     8     -2       0     1     -1     -3     1     0     -2     10       -4     -3     -4     -2     -3     -4     -4     -4       -3     -4     -4     -2     -2     -3     -4     -3       3     0     -1     -3     2     1     -2     0       -2     -2     -4     -2     0     -2     -3     -1       -3     -4     -5     -2     -4     -3     -4     -1       -3     -2     -1     -4     -1     -1     -2     -2       -1     1     0     -1     0     -1     0     -1       -1     0     -1     -1     -1     -1     -2     -2       -3     -4     -5     -5     -1     -3     -3     -3       -1     -2     -3     -3     -1     -2     -3     2       -3     -3     -4     -1     -3     -3     -4     -4       -1     -2     -3     -3< | 0         0         2         -3         2         6         -3         0         -4           -3         0         -1         -3         -2         -3         8         -2         -4           0         1         -1         -3         1         0         -2         10         -4           -4         -3         -4         -2         -3         -4         -4         -5           -3         -4         -4         -2         -2         -3         -4         -3         2           -3         -4         -4         -2         -2         -3         -4         -3         2           -3         -4         -4         -2         -2         -3         -4         -3         2           -3         -4         -5         -2         -4         -3         -4         -1         0           -3         -4         -5         -2         -4         -3         -4         -1         0           -3         -2         -1         -4         -1         -1         -2         -2         -3           -1         0         -1         -1 | 0         0         2         -3         2         6         -3         0         -4         -3           -3         0         -1         -3         -2         -3         8         -2         -4         -4            0         1         -1         -3         1         0         -2    
    10         -4         -3           -4         -3         -4         -2         -3         -4         -4         -4         5         2           -3         -4         -4         -2         -2         -3         -4         -3         2         5           3         0         -1         -3         2         1         -2         0         -3         -3           -2         -2         -4         -2         0         -2         -3         -1         2         3           -3         -4         -5         -2         -4         -3         -4         -1         0         1           -3         -4         -5         -2         -4         -3         -4         -1         0         1           -3         -4         -5         -5 <td< th=""><th>0         0         2         -3         2         6         -3         0         -4         -3         1           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2           0         1         -1         -3         1         0         -2         10         -4         -3         0           -4         -3         -4         -2         -3         -4         -4         -5         2         -3           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3           3         0         -1         -3         2         1         -2         0         -3         -3         6           -2         -2         -4         -2         0         -2         -3         -1         2         3         -2           -3         -4         -5         -2         -4         -3         -4         -1         0         1         -4           -3         -2         -1         -4         -1         -1         -1         -1         <td< th=""><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2         -3           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1           -4         -3         -4         -2         -2         -3         -4         -4         -5         2         -3         2           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3         3           3         0         -1         -3         2         1         -2         0         -3         -3         6         -2           -2         -2         -4         -2         0         -2         -3         -1         2         3         -2         7           -3         -4         -5         -2         -4         -3         -4         -1         0         1         -4         0</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -4         -4         -2         -3         -4         -4         -2         -3         -4         -4         -2         -3         -4         -4         -2         -3         -1         -2         -2         -3         -4         -1         -3         -4         -1         -3         -4         -1         -3         -4         -1         -3         -4         -1         -3         -3</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2           -4         -3         -4         -2         -3         -4         -4         -4         5         2         -3         2         0         -3           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3         3         1         -4           3         0         -1         -3         2         1         -2         0         -3         -3         6         -2         -4         -1           -2         -2         -4         -2         0         -2         -3         -1         2         3         -2         7         0         -3</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1           -4         -3         -4         -2         -3         -4         -4         -4         5         2         -3         2         0         -3         -3           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3         3         1         -4         -3           3         0         -1         -3         2         1         -2         0         -3         -3         6         -2         -4         -1         0           -2         -2         -4         -3         -1         2         3         -</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -2         0         -2         -1         -2         -3         -4         -2         -2         -1         -2         -1         -2         -1         -2         -1         -2         -1         -2         -3         -3         -1         -2         -3         -1         -3         -1         -3         -4         -3         -1         -3         -4         -3         -1         -3         -3         -1         -3         -1         -3         -1         -3         -1         -3         -1         -3         -1         -3         -2         -1         -1         -1         -1         -1         -1         -1</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -1         -3         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -4         -2         0         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -3         -3         -1         -3         -4         -3         -2         -3         2         0         -3         -3         -1         -2         -3         -1         -3         -4         -3         -1         -2         -2         -4         -1         0         -1         -3         -1         -2         -2         -4         -1         0         -1         -3         -2         -1         -1         -1         -1         &lt;</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -3           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1         -2         -3         2           -4         -3         -4         -4         -4         5         2         -3         2         0         -3         -3         -1         -3         -1         -3         -1         -2         -1         -3         -1         -2         -1         -3         -1         -2         -3         -3         1         -4         -3         -1         -2         -1           -3         -4         -4         -2         -2         -3         -1         2         3         -2         7         0         -3         -2         -1         -1         0</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -4           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1         -2         -3         2         -4           -4         -3         -4         -2         -3         -4         -4         -4         5     
   2         -3         2         0         -3         -3         -1         -2         -1         1           -3         -4         -4         -2         -2         -3         -4         -3         -2         -3         3         1         -4         -3         -1         -2         -1         1           3         0         -1         -3         -3         -3         -2         -4         -1         0         -1         -3         -2</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -4         -1           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1         -2         -3         2         -4         0           -4         -3         -4         -2         -3         -4         -4         -4         -5         2         -3         2         0         -3         -3         -1         -3         -1         -4         -3         -1         -2         -1         1         -4         -3         -1         -2<th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         1         -2         -3         -1         -1         -3         -2         -3         -4         -1         -2         0         -2         -3         -3         -4         -1         -2         0         -2         -3         -3         -4         -1         -2         0         0         -2         -3         -3         0         -1         -1         -2         -3         2         -4         0         0         0         -2         -3         -4         -4         -3         0         -1         -2         -3         2         -4         0         0         0         -4         -3         -2         -1         -1         0</th><th>  0</th></th></td<></th></td<> | 0         0         2         -3         2         6         -3         0         -4         -3         1           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2           0         1         -1         -3         1         0         -2         10         -4         -3         0           -4         -3         -4         -2         -3         -4         -4         -5         2         -3           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3           3         0         -1         -3         2         1         -2         0         -3         -3         6           -2         -2         -4         -2         0         -2         -3         -1         2         3         -2           -3         -4         -5         -2         -4         -3         -4         -1         0         1         -4           -3         -2         -1         -4         -1         -1         -1         -1 <td< th=""><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2         -3           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1           -4         -3         -4         -2         -2         -3         -4         -4         -5         2         -3         2           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3         3           3         0         -1         -3         2         1         -2         0         -3         -3         6         -2           -2         -2         -4         -2         0         -2         -3         -1         2         3         -2         7           -3         -4         -5         -2         -4         -3         -4         -1         0         1         -4         0</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -4         -4         -2         -3         -4         -4         -2         -3         -4         -4         -2         -3         -4         -4         -2         -3         -1         -2         -2         -3         -4         -1         -3         -4         -1         -3         -4         -1         -3         -4         -1         -3         -4         -1         -3         -3</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2           -4         -3         -4         -2         -3         -4         -4         -4         5         2         -3         2         0         -3           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3         3         1         -4           3         0         -1         -3         2         1         -2         0         -3         -3         6         -2         -4         -1           -2         -2         -4         -2         0         -2         -3         -1         2         3         -2         7         0         -3</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1           -4         -3         -4         -2         -3         -4         -4         -4         5         2         -3         2         0         -3         -3           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3         3         1         -4         -3           3         0         -1         -3         2         1         -2         0         -3         -3         6         -2         -4         -1         0           -2         -2         -4         -3         -1         2         3         -</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -2         0         -2         -1         -2         -3         -4         -2         -2         -1         -2         -1         -2         -1         -2         -1         -2         -1         -2         -3         -3         -1         -2         -3         -1         -3         -1         -3         -4         -3         -1         -3         -4         -3         -1         -3         -3         -1         -3         -1         -3         -1         -3         -1         -3         -1         -3         -1         -3         -2         -1         -1         -1         -1         -1         -1         -1</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -1         -3         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -4         -2         0         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -3         -3         -1         -3         -4         -3         -2         -3         2         0         -3         -3         -1         -2         -3         -1         -3         -4         -3         -1         -2         -2        
-4         -1         0         -1         -3         -1         -2         -2         -4         -1         0         -1         -3         -2         -1         -1         -1         -1         &lt;</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -3           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1         -2         -3         2           -4         -3         -4         -4         -4         5         2         -3         2         0         -3         -3         -1         -3         -1         -3         -1         -2         -1         -3         -1         -2         -1         -3         -1         -2         -3         -3         1         -4         -3         -1         -2         -1           -3         -4         -4         -2         -2         -3         -1         2         3         -2         7         0         -3         -2         -1         -1         0</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -4           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1         -2         -3         2         -4           -4         -3         -4         -2         -3         -4         -4         -4         5         2         -3         2         0         -3         -3         -1         -2         -1         1           -3         -4         -4         -2         -2         -3         -4         -3         -2         -3         3         1         -4         -3         -1         -2         -1         1           3         0         -1         -3         -3         -3         -2         -4         -1         0         -1         -3         -2</th><th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -4         -1           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1         -2         -3         2         -4         0           -4         -3         -4         -2         -3         -4         -4         -4         -5         2         -3         2         0         -3         -3         -1         -3         -1         -4         -3         -1         -2         -1         1         -4         -3         -1         -2<th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         1         -2         -3         -1         -1         -3         -2         -3         -4         -1         -2         0         -2         -3         -3         -4         -1         -2         0         -2         -3         -3         -4         -1         -2         0         0         -2         -3         -3         0         -1         -1         -2         -3         2         -4         0         0         0         -2         -3         -4         -4         -3         0         -1         -2         -3         2         -4         0         0         0         -4         -3         -2         -1         -1         0</th><th>  0</th></th></td<> | 0         0         2         -3         2         6         -3         0         -4         -3         1         -2           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2         -3           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1           -4         -3         -4         -2         -2         -3         -4         -4         -5         2         -3         2           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3         3           3         0         -1         -3         2         1         -2         0         -3         -3         6         -2           -2         -2         -4         -2         0         -2         -3         -1         2         3         -2         7           -3         -4         -5         -2         -4         -3         -4         -1         0         1         -4         0 | 0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -4         -4         -2         -3         -4         -4         -2         -3         -4         -4         -2         -3         -4         -4         -2         -3         -1         -2         -2         -3         -4         -1         -3         -4         -1         -3         -4         -1         -3         -4         -1         -3         -4         -1         -3         -3 | 0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2           -4         -3         -4         -2         -3         -4         -4         -4         5         2         -3         2         0         -3           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3         3         1         -4           3         0         -1         -3         2         1         -2         0         -3         -3         6         -2         -4         -1           -2         -2         -4         -2         0         -2         -3         -1         2         3         -2         7         0         -3 | 0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1           -3         0         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1           -4         -3         -4         -2         -3         -4         -4         -4         5         2         -3         2         0         -3         -3           -3         -4         -4         -2         -2         -3         -4         -3         2         5         -3         3         1         -4         -3           3         0         -1         -3         2         1         -2         0         -3         -3         6         -2         -4         -1         0           -2         -2         -4         -3         -1         2         3         - | 0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -2         0         -2         -1         -2         -3         -4         -2         -2         -1         -2         -1         -2         -1         -2         -1         -2         -1         -2         -3         -3         -1         -2         -3         -1         -3         -1         -3         -4         -3         -1         -3         -4         -3         -1         -3         -3         -1         -3         -1         -3         -1         -3         -1         -3         -1         -3         -1         -3         -2         -1         -1         -1         -1         -1         -1         -1 | 0         0         2         -3         2         6         -3         0       
 -4         -3         1         -2         -3         -1         -1         -1         -3         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -4         -2         0         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -2         -3         -3         -1         -3         -3         -1         -3         -4         -3         -2         -3         2         0         -3         -3         -1         -2         -3         -1         -3         -4         -3         -1         -2         -2         -4         -1         0         -1         -3         -1         -2         -2         -4         -1         0         -1         -3         -2         -1         -1         -1         -1         < | 0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -3           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1         -2         -3         2           -4         -3         -4         -4         -4         5         2         -3         2         0         -3         -3         -1         -3         -1         -3         -1         -2         -1         -3         -1         -2         -1         -3         -1         -2         -3         -3         1         -4         -3         -1         -2         -1           -3         -4         -4         -2         -2         -3         -1         2         3         -2         7         0         -3         -2         -1         -1         0 | 0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -4           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1         -2         -3         2         -4           -4         -3         -4         -2         -3         -4         -4         -4         5         2         -3         2         0         -3         -3         -1         -2         -1         1           -3         -4         -4         -2         -2         -3         -4         -3         -2         -3         3         1         -4         -3         -1         -2         -1         1           3         0         -1         -3         -3         -3         -2         -4         -1         0         -1         -3         -2 | 0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         8         -2         -4         -4         -2         -3         -4         -2         0         -2         -3         -4         -1           0         1         -1         -3         1         0         -2         10         -4         -3         0         -1         -1         -2         -1         -2         -3         2         -4         0           -4         -3         -4         -2         -3         -4         -4         -4         -5         2         -3         2         0         -3         -3         -1         -3         -1         -4         -3         -1         -2         -1         1         -4         -3         -1         -2 <th>0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         1         -2         -3         -1         -1         -3         -2         -3         -4         -1         -2         0         -2         -3         -3         -4         -1         -2         0         -2         -3         -3         -4         -1         -2         0         0         -2         -3         -3         0         -1         -1         -2         -3         2         -4         0         0         0         -2         -3         -4         -4         -3         0         -1         -2         -3         2         -4         0         0         0         -4         -3         -2         -1         -1         0</th> <th>  0</th> | 0         0         2         -3         2         6         -3         0         -4         -3         1         -2         -3         -1         -1         -3         -2         -3         1         -2         -3         -1         -1         -3         -2         -3         -4         -1         -2         0         -2         -3         -3         -4         -1         -2         0         -2         -3         -3         -4         -1         -2         0         0         -2         -3         -3         0         -1         -1         -2         -3         2         -4         0         0         0         -2         -3         -4         -4         -3         0         -1         -2         -3         2         -4         0         0         0         -4         -3         -2         -1         -1         0 | 0  |

### Local vs. Global Alignment

 The <u>Global Alignment Problem</u> tries to find the longest path between vertices (0,0) and (n,m) in the edit graph.

 The <u>Local Alignment Problem</u> tries to find the longest path among paths between **arbitrary vertices** (*i*,*j*) and (*i*', *j*') in the edit graph.

#### Local vs. Global Alignment

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- The <u>Local Alignment Problem</u> tries to find the longest path among paths between **arbitrary vertices** (*i*,*j*) and (*i*', *j*') in the edit graph.
- In the edit graph with negatively-scored edges, Local Alignmet may score higher than Global Alignment

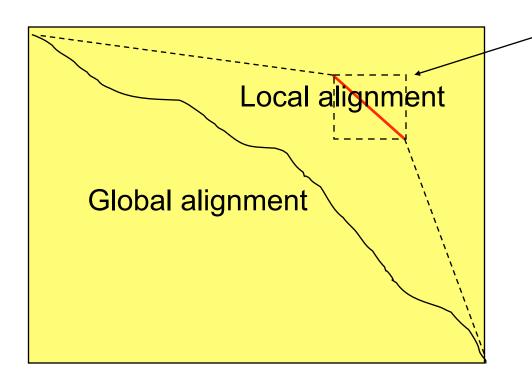
#### Local vs. Global Alignment (cont'd)

Global Alignment

 Local Alignment—better alignment to find conserved segment

tccCAGTTATGTCAGgggacacgagcatgcagagac

aattgccgccgtcgttttcagCAGTTATGTCAGatc



Compute a "mini"
Global Alignment to
get Local

## Local Alignments: Why?

- Two genes in different species may be similar over short conserved regions and dissimilar over remaining regions.
- Example:
  - Homeobox genes have a short region called the *homeodomain* that is highly conserved between species.
  - A global alignment would not find the homeodomain because it would try to align the ENTIRE sequence

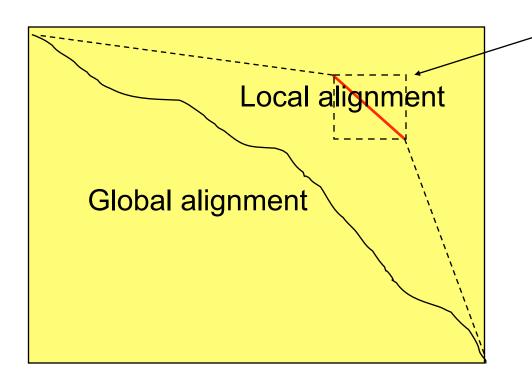
#### The Local Alignment Problem

- Goal: Find the best local alignment between two strings
- Input: Strings v, w and scoring matrix δ
- Output: Alignment of substrings of v and w whose alignment score is maximum among all possible alignment of all possible substrings

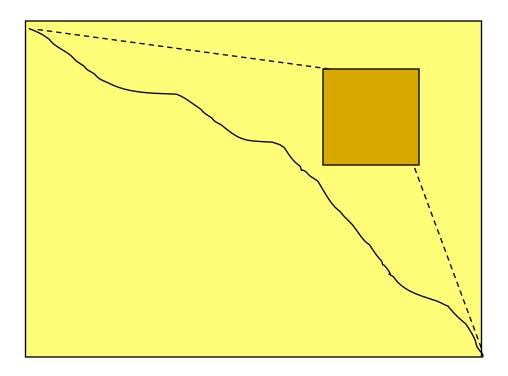
#### The Problem with this Problem

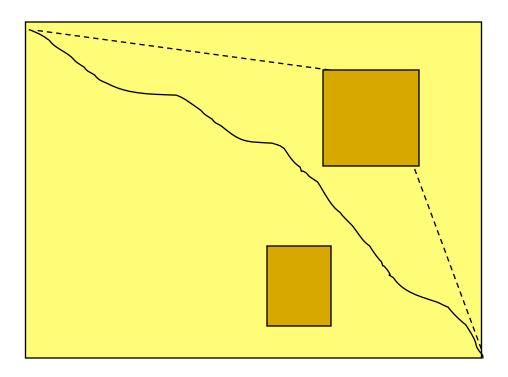
• Long run time O(n<sup>4</sup>):

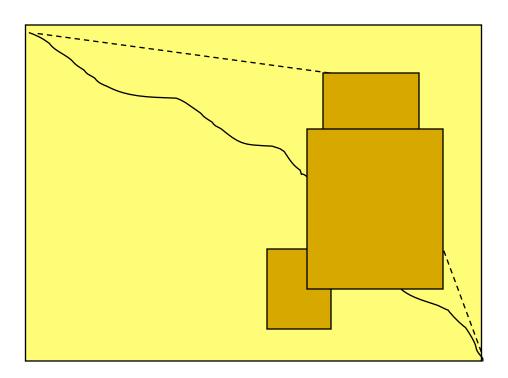
- In the grid of size  $n \times n$  there are  $\sim n^2$  vertices (i,j) that may serve as a source.
- For each such vertex computing alignments from (i,j) to (i',j') takes  $O(n^2)$  time.
- This can be remedied by giving free rides

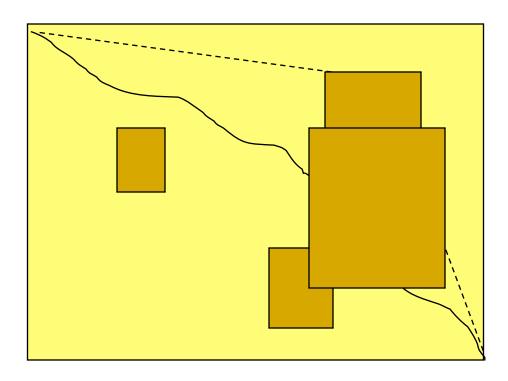


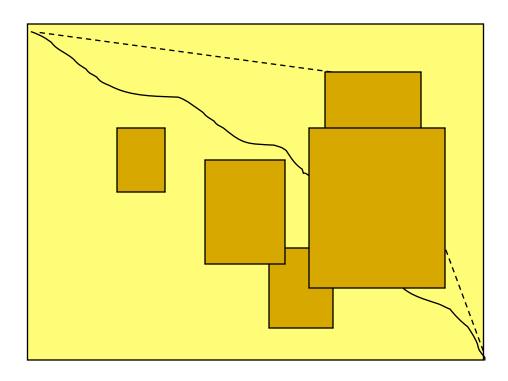
Compute a "mini"
Global Alignment to
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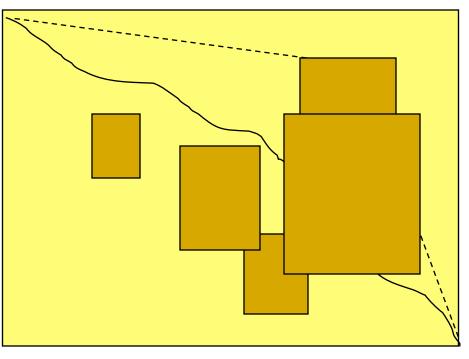






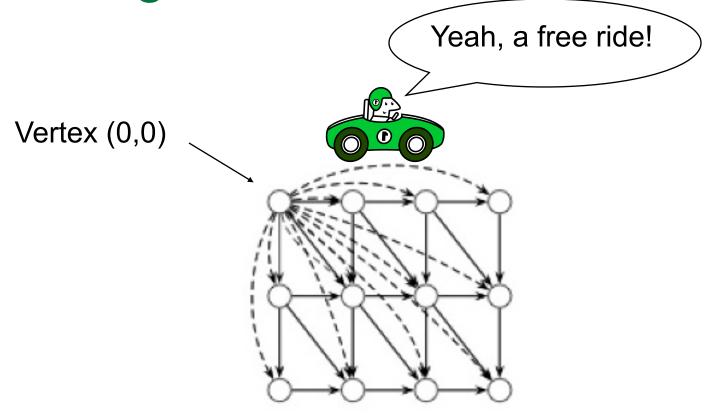


## Local Alignment: Running Time



- Long run time  $O(n^4)$ :
  - In the grid of size  $n \times n$  there are  $\sim n^2$  vertices (i,j) that may serve as a source.
  - For each such vertex computing alignments from (i,j) to (i',j') takes  $O(n^2)$  time.
- This can be remedied by giving free rides

Local Alignment: Free Rides



The dashed edges represent the free rides from (0,0) to every other node.

### The Local Alignment Recurrence

• The largest value of  $s_{i,j}$  over the whole edit graph is the score of the best local alignment.

• The recurrence:

Notice there is only this change from the 
$$s_{i,j} = max$$
  $s_{i-1,j-1} + (v_i, w_j)$  riginal recurrence of  $\begin{cases} s_{i-1,j} + (v_i, -) & \text{a Global Alignment} \\ s_{i,j-1} + (-, w_j) \end{cases}$ 

### The Local Alignment Recurrence

• The largest value of  $s_{i,j}$  over the whole edit graph is the score of the best local alignment.

#### • The recurrence:

$$S_{i,j} = max \quad S_{i-1,j-1} + (v_i, w_j)$$

$$\begin{cases} S_{i-1,j} + (v_i, -) \\ S_{i,j-1} + (-, w_j) \end{cases}$$

Power of ZERO: there is only this change from the original recurrence of a Global Alignment - since there is only one "free ride" edge entering into every vertex

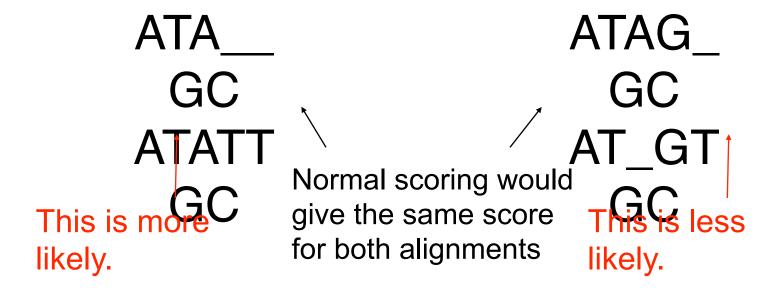
#### Scoring Indels: Naive Approach

- A fixed penalty σ is given to every indel:
  - σ for 1 indel,
  - -2σ for 2 consecutive indels
  - -3σ for 3 consecutive indels, etc.

Can be too severe penalty for a series of 100 consecutive indels

### Affine Gap Penalties

 In nature, a series of k indels often come as a single event rather than a series of k single nucleotide events:



### Accounting for Gaps

- Gaps- contiguous sequence of spaces in one of the rows
- Score for a gap of length x is:

$$-(\rho + \sigma x)$$

where  $\rho > 0$  is the penalty for introducing a gap:

gap opening penalty

ρ will be large relative to σ:

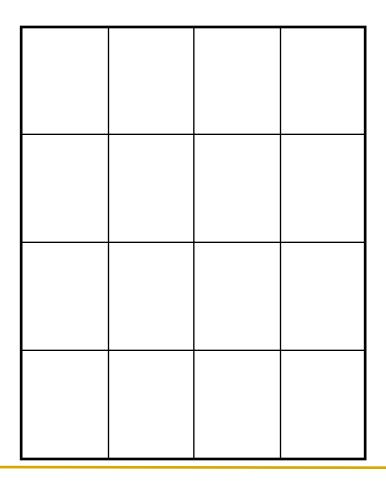
gap extension penalty

because you do not want to add too much of a penalty for extending the gap.

#### Affine Gap Penalties

- Gap penalties:
  - $-\rho$ - $\sigma$  when there is 1 indel
  - $-\rho$ -2 $\sigma$  when there are 2 indels
  - $-\rho$ -3 $\sigma$  when there are 3 indels, etc.
  - - $\rho$  x- $\sigma$  (-gap opening x gap extensions)
- Somehow reduced penalties (as compared to naïve scoring) are given to runs of horizontal and vertical edges

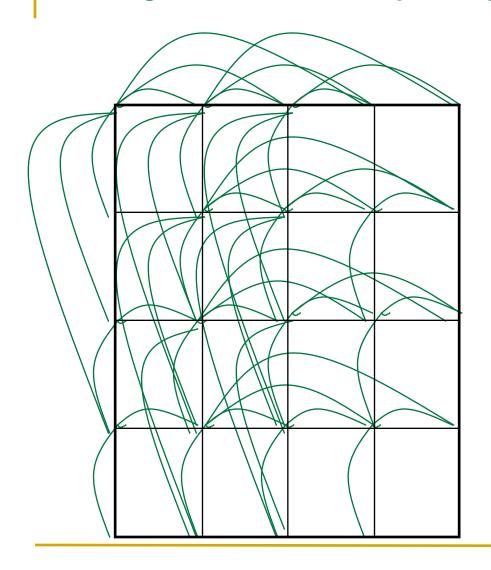
#### Affine Gap Penalties and Edit Graph



To reflect affine gap penalties we have to add "long" horizontal and vertical edges to the edit graph. Each such edge of length *x* should have weight

-r - x \*s

#### Adding "Affine Penalty" Edges to the Edit Graph

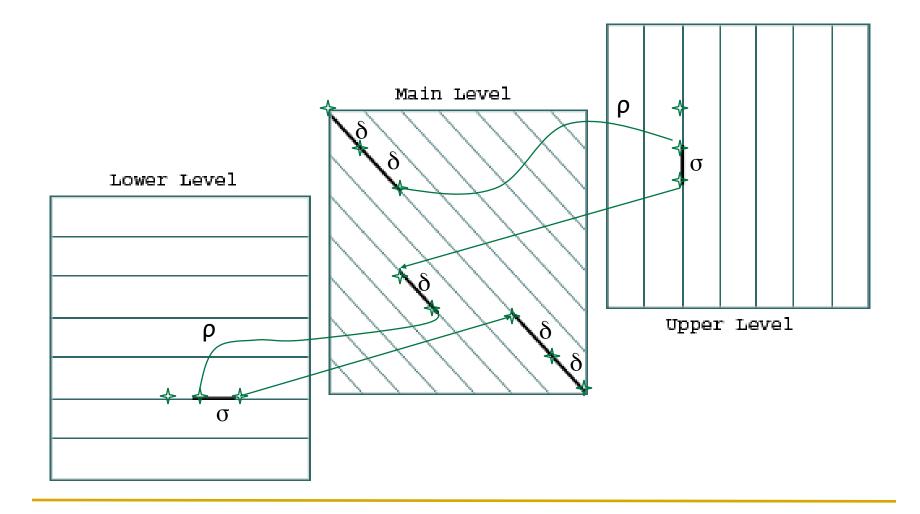


There are many such edges!

Adding them to the graph increases the running time of the alignment algorithm by a factor of *n* (where *n* is the number of vertices)

So the complexity increases from  $O(n^2)$  to  $O(n^3)$ 

## Manhattan in 3 Layers



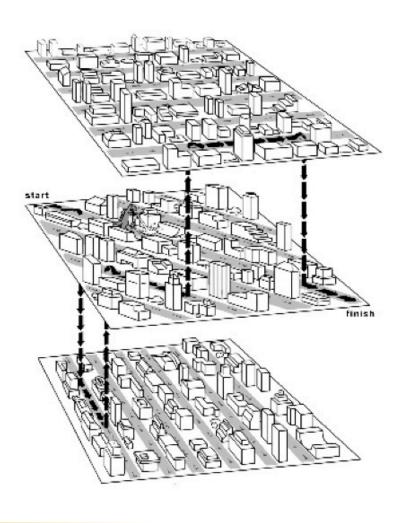
#### Affine Gap Penalties and 3 Layer Manhattan Grid

- The three recurrences for the scoring algorithm creates a 3-layered graph.
- The top level creates/extends gaps in the sequence w.
- The bottom level creates/extends gaps in sequence v.
- The middle level extends matches and mismatches.

#### Switching between 3 Layers

- Levels:
  - The main level is for diagonal edges
  - The lower level is for horizontal edges
  - The upper level is for vertical edges
- A jumping penalty is assigned to moving from the main level to either the upper level or the lower level (-r-s)
- There is a gap extension penalty for each continuation on a level other than the main level (-s)

#### The 3-leveled Manhattan Grid



Gaps in w

Matches/
Mismatch
es
Gaps in v

#### Affine Gap Penalty Recurrences

$$\begin{array}{rcl}
\downarrow \\
s_{i,j} &= \begin{cases}
\downarrow \\
s_{i-1,j} - \sigma \\
s_{i-1,j} - (\rho + \sigma)
\end{cases}$$

Continue Gap in w (deletion) Start Gap in w (deletion): from middle

$$\overrightarrow{s_{i,j}} = \begin{cases} \overrightarrow{s_{i,j-1}} - \sigma \\ s_{i,j-1} - (\rho + \sigma) \end{cases}$$

Continue Gap in *v* (insertion)

Start Gap in *v* (insertion):from middle

 $s_{i,j} = \begin{cases} s_{i-1,j-1} + \delta & \text{Match or Mismatch} \\ s_{i,j} + \delta & \text{with added to max} \end{cases}$ End insertion: from both

End insertion: from bottom